



Modelling Birth Rate in Otuoke, Bayelsa State, Nigeria: A Time Series Approach

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Estimation

Abstract

This study seeks to determine a suitable Time series model for predicting birthrate in Bayelsa State, Nigeria, using Time series Box- Jenkins method. Monthly birth data from April, 2015 to April 2022 collected from Federal Medical Centre Otuoke Bayelsa State was used. The Augmented Dick Fuller test was used to test for unit root. The unit root test revealed that the data was not stationary. The series was difference and stationary at the first differencing. Based on of various selection criteria Autoregressive Integrated Moving Average, ARIMA (1, 1, 1) was identified as an appropriate model for the forecast of birthrate. The Ljung-Box Q test used to test the adequacy of the model. The residual of the model was checked using Ljung-Box residual test and it shows no sign of autocorrelation in the residual. Thus, Autoregressive Integrated Moving Average ARIMA (1,1,1) model was recommended for forecast of birth-rate in Bayelsa state.

*Corresponding Author: Eli, I.C.; eliic@fuotuoke.edu.ng**Introduction**

Forecasts of monthly births can help predict the fluctuating trends of a country's population distribution, which is also important in estimating the increase in population. The importance of population forecasting in the context of national, state, and local government budgeting and legislation in medical services, security, and infrastructure cannot be emphasized (Bravo and Magalhães, 2010). To appropriately design programs to reduce mortality among kids and fertility, it is also necessary to understand the concept of birth rate, especially among developing nations experiencing population change (Soest & Saha, 2018). Several independent studies have found a link between particular periodic birth rates, reproductive customs, and the risk of a child dying (Asefa *et al.*, 2000).

Research findings indicate the occurrence of seasonal and trend patterns in birth rate data. As a result, utilizing models based on time series to forecast birth and mortality rates has grown in popularity in the past few decades. A time series is any random variable that is observed sequentially throughout time. Analyzing time series data requires analyzing the characteristics of

the response variable with respect to time as the independent variable.

The time variable is used as a point of reference for estimating the target variable for predicting or forecasting purposes. Hussein (1993), for example, analyzed Egypt's crude birth rate and crude death rate from 1992 to 2010 employing the autoregressive integrated moving average (ARIMA) model; the study used a time series approach to anticipate Egypt's rates of births and deaths beyond 2010. Furthermore, Adsera (2006), Abel *et al.* (2013), Lee (1992), Ahlo (2012), Lee and Tuljapurkar (1994), Graham *et al.* (2008), Keilman *et al.* (2002), Tayman (2007), Kirk (1996), Rau (2007), Palloni, and Rafalimanana (1999) amongst others have also worked on the application of time series models for birth rate and demographic forecasting.

The autoregressive integrated moving average (ARIMA) is one of the time series models commonly used. The model is also known as the ARIMA (p, d, q) model, where p is the autoregressive component, q is the moving average component and d represents differencing, p, d and q are all integers larger than or equal to 1. The ARIMA model is appropriate when the

data is stationary. For a stationary series, the mean, variance and autocorrelation function remain constant throughout time.

The evaluation of time series models for birth and death in Otuoke has received little attention thus, the main focus of the present study is to determine a suitable ARIMA model for the forecast monthly Birth

rate in Otuoke, Bayelsa State, Nigeria using the time series method developed by Box- Jenkins.

Materials and Methods

Autoregressive (AR) Model

The autoregressive process of order k denoted by AR(k) is a time series model given by

$$X_t = \sum_{i=1}^k \vartheta_i X_{t-i} + \varepsilon_t$$

$$= \vartheta_1 X_{t-1} + \vartheta_2 X_{t-2} + \vartheta_3 X_{t-3} + \dots + \vartheta_k X_{t-k} + \varepsilon_t \quad (1)$$

Where the ϑ_i $i = 1, 2, 3, \dots, k$ are the model parameters and ε_t is a sequence of independently and identically distributed (iid) random variables with $E(\varepsilon_t) = 0$ and $var(\varepsilon_t) = \sigma_e^2$

Autoregressive models are based on the idea that the current value of the series, can be explained as a linear combination of past values, together with a random error in the same series.

Moving Average (MA) Model

Given that ε_t is a sequence of independently and identically distributed (iid) random variables with $E(\varepsilon_t) = 0$ and $var(\varepsilon_t) = \sigma_e^2$, then

$$X_t = \sum_{i=1}^r \theta_i \varepsilon_{t-i} = \theta_1 \varepsilon_{t-1} + \theta_2 \varepsilon_{t-2} + \theta_3 \varepsilon_{t-3} + \dots + \theta_r \varepsilon_{t-r} \quad (2)$$

is the r th order moving average MA(r) model.

Autoregressive Moving Average (ARMA) Model

Autoregressive Moving Average (ARMA) Model is a mixture of the AR and MA models. Thus, a time series is said to follow an autoregressive moving-average process of order k and r , i.e ARMA (k, r), process if:

$$X_t = \sum_{i=1}^k \vartheta_i X_{t-i} + \varepsilon_t + \sum_{i=1}^r \theta_i \varepsilon_{t-i}$$

$$X_t = \vartheta_1 X_{t-1} + \vartheta_2 X_{t-2} + \vartheta_3 X_{t-3} + \dots + \vartheta_k X_{t-k} + \varepsilon_t + \theta_1 \varepsilon_{t-1} + \theta_2 \varepsilon_{t-2} + \theta_3 \varepsilon_{t-3} + \dots + \theta_r \varepsilon_{t-r} \quad (3)$$

$$X_t - \vartheta_1 X_{t-1} - \vartheta_2 X_{t-2} - \vartheta_3 X_{t-3} - \dots - \vartheta_k X_{t-k} = \varepsilon_t + \theta_1 \varepsilon_{t-1} + \theta_2 \varepsilon_{t-2} + \theta_3 \varepsilon_{t-3} + \dots + \theta_r \varepsilon_{t-r}$$

$$(1 - \vartheta_1 B - \vartheta_2 B^2 - \vartheta_3 B^3 - \dots - \vartheta_k B^k) X_t = (1 - \theta_1 B - \theta_2 B^2 - \theta_3 B^3 - \dots - \theta_r B^r) \varepsilon_t$$

$$\vartheta(B) X_t = \theta(B) \varepsilon_t$$

Where $\vartheta(B) = 1 - \vartheta_1 B - \vartheta_2 B^2 - \vartheta_3 B^3 - \dots - \vartheta_k B^k$ and $\theta(B) = 1 - \theta_1 B - \theta_2 B^2 - \theta_3 B^3 - \dots - \theta_r B^r$, the backward shift; $B^k X_t = X_{t-k}$

Frequently, after achieving stationarity, time series models contain AR(k) and MA(r) of certain orders which in combination could be used for forecast. The model is usually referred to as the ARMA (k, r) process where k is the order of the autoregressive part and r is the order of the moving average part.

ARIMA Models

The ARIMA models can further be extended to non-stationary series by allowing the differencing of the data series resulting in ARIMA models. The general non-seasonal model is known as ARIMA (k, d, r): where with three parameters; k is the order of autoregressive, d is the degree of differencing, and r is the order of moving average. The ARIMA(k,d,r) model is denoted as follows:

$$\vartheta(B)\nabla^d X_t = \theta(B)\varepsilon_t$$

Where $\nabla(B) = 1 - B$ is the differencing parameter applied d times, and d is a non-negative integer.

$$\vartheta(B) = 1 - \sum_{i=1}^r \vartheta_i B^i \text{ and } \vartheta(B) \text{ is the AR operator}$$

$$\theta(B) = 1 - \sum_{j=1}^r \theta_j B^j \text{ and } \theta(B) \text{ is the MA operator}$$

Data

The data used in this work are of secondary sources. The comprised of monthly birth rate in federal medical center Otueke, Bayelsa State, Nigeria from April 2015 to April 2022.

Test for stationarity:

The ARIMA model is suitable for stationary time series data, thus, a test for stationarity (unit root test) of the data is necessary before further analysis. The unit root test for the data was carried out using the Augmented Dick Fuller (ADF) Test.

Results

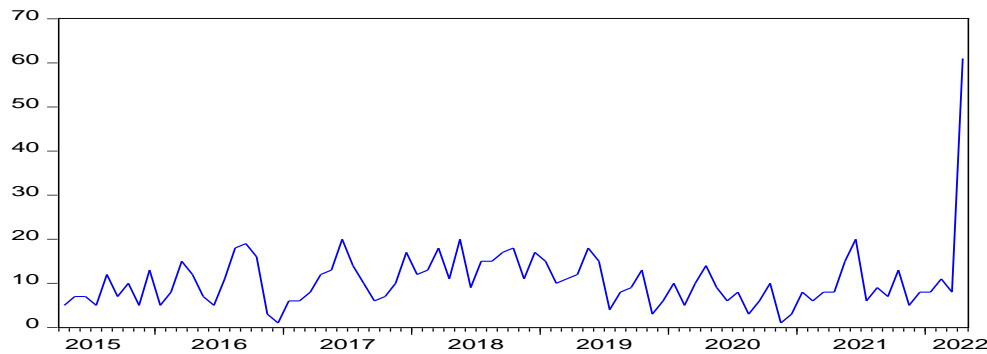


Fig.1 Time Plot of Birth Rate

Table 1: Unit Root Test of Monthly Birth Series

Null Hypothesis: MONTHLYBIRTH has a unit root
 Exogenous: Constant
 Lag Length: 0 (Automatic - based on SIC, maxlag=11)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-4.139385	0.0614
Test critical values: 1% level	-3.510259	
5% level	-2.896346	
10% level	-2.585396	

*MacKinnon (1996) one-sided p-values.

Augmented Dickey-Fuller Test Equation
 Dependent Variable: D(MONTHLYBIRTH)
 Method: Least Squares
 Date: 11/06/23 Time: 20:42
 Sample (adjusted): 2015M05 2022M04
 Included observations: 84 after adjustments

Variable	Coefficient	Std. Error	t-Statistic	Prob.
MONTHLYBIRTH (-1)	-0.710488	0.171641	-4.139385	0.0001
C	7.822300	1.892134	4.134115	0.0001
R-squared	0.172841	Mean dependent var		0.666667
Adjusted R-squared	0.162754	S.D. dependent var		7.705941
S.E. of regression	7.051026	Akaike info criterion		6.767745
Sum squared resid	4076.791	Schwarz criterion		6.825621
Log-likelihood	-282.2453	Hannan-Quinn criter.		6.791011
F-statistic	17.13451	Durbin-Watson stat		1.384478
Prob(F-statistic)	0.000084			

Table 1 shows the ADF result for the monthly birthrate data, demonstrating the nonstationary nature of the data. The data was differenced and the plot of the first difference is given in figure2 below

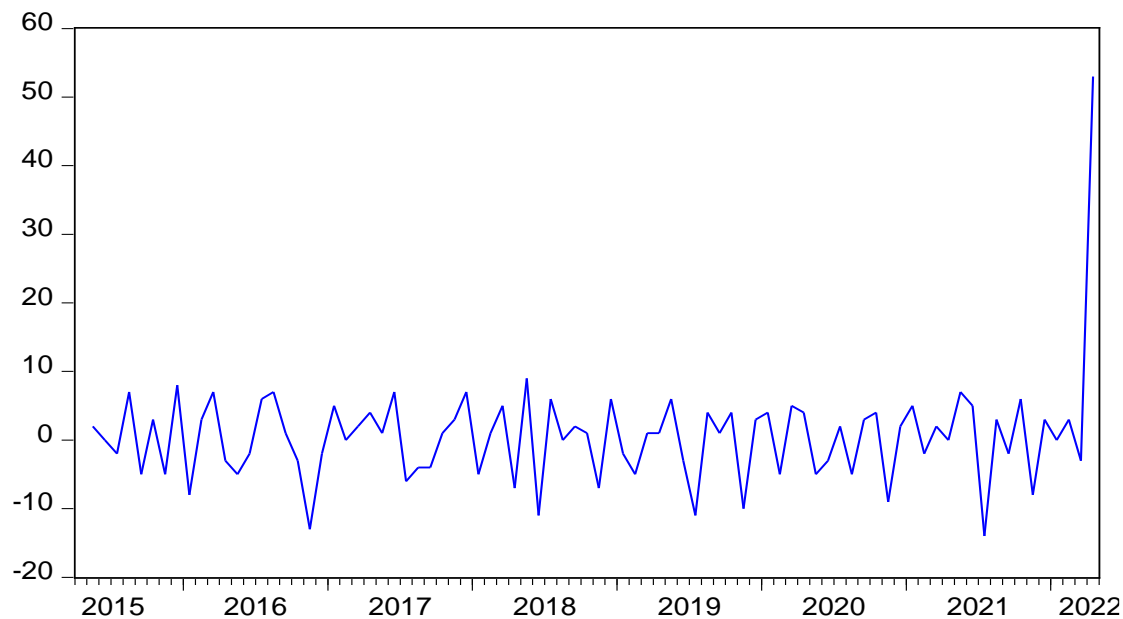


Fig.2: Time Plot of the first difference

Table 2: Unit root test for the differenced series.

Null Hypothesis: D(DMONTHLYBIRTH) has a unit root

Exogenous: Constant

Lag Length: 2 (Automatic - based on SIC, maxlag=11)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-8.025997	0.0000
Test critical values:		
1% level	-3.514426	
5% level	-2.898145	
10% level	-2.586351	

*MacKinnon (1996) one-sided p-values.

Augmented Dickey-Fuller Test Equation

Dependent Variable: D(DMONTHLYBIRTH,2)

Method: Least Squares

Date: 11/06/23 Time: 20:50

Sample (adjusted): 2015M09 2022M04

Included observations: 80 after adjustments

Variable	Coefficient	Std. Error	t-Statistic	Prob.
D(DMONTHLYBIRTH(-1))	-3.228095	0.402205	-8.025997	0.0000
D(DMONTHLYBIRTH(-1),2)	1.191971	0.297880	4.001510	0.0001
D(DMONTHLYBIRTH(-2),2)	0.443130	0.146787	3.018868	0.0035
C	0.579052	0.926766	0.624809	0.5340
R-squared	0.759483	Mean dependent var		0.587500
Adjusted R-squared	0.749989	S.D. dependent var		16.57793
S.E. of regression	8.289154	Akaike info criterion		7.116480
Sum squared resid	5221.966	Schwarz criterion		7.235581
Log likelihood	-280.6592	Hannan-Quinn criter.		7.164231
F-statistic	79.99517	Durbin-Watson stat		1.575921
Prob(F-statistic)	0.000000			

Table 2 shows that the Augmented Dickey-Fuller test, at the first difference, is 0.00. Thus, the series is considered to be stationary at the first differencing. We can progress to determine a suitable model for the series.

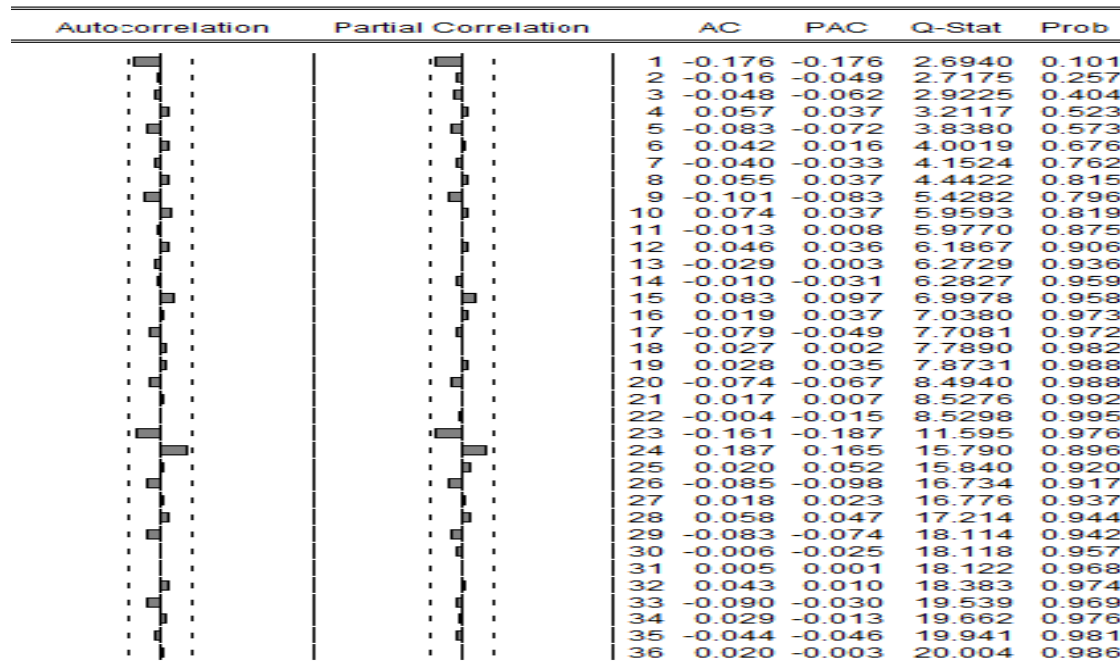


Fig.3 Correlogram of birth rate data after first difference

Table 3 Estimate of ARIMA Model

Dependent Variable: DMONTHLYBIRTH
 Method: ARMA Maximum Likelihood (OPG - BHHH)
 Date: 11/14/23 Time: 08:55
 Sample: 2015M05 2022M04
 Included observations: 84
 Convergence achieved after 23 iterations

Coefficient covariance computed using an outer product of gradients

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	0.142059	0.272340	0.521622	0.6034
AR(1)	0.206107	0.382689	0.538575	0.0007
MA(1)	-0.857705	0.193780	-4.426189	0.0000
SIGMASQ	50.05519	3.705391	13.50875	0.0000
R-squared	0.146902	Mean dependent var		0.666667
Adjusted R-squared	0.114911	S.D. dependent var		7.705941
S.E. of regression	7.249686	Akaike info criterion		6.857966
Sum squared resid	4204.636	Schwarz criterion		6.973719
Log likelihood	-284.0346	Hannan-Quinn criter.		6.904498
F-statistic	4.591952	Durbin-Watson stat		1.383635
Prob(F-statistic)	0.005117			
Inverted AR Roots	.21			
Inverted MA Roots	.86			

Date: 11/14/23 Time: 08:50
 Sample: 2015M04 2022M04
 Included observations: 84
 Q-statistic probabilities adjusted for 2 ARMA terms

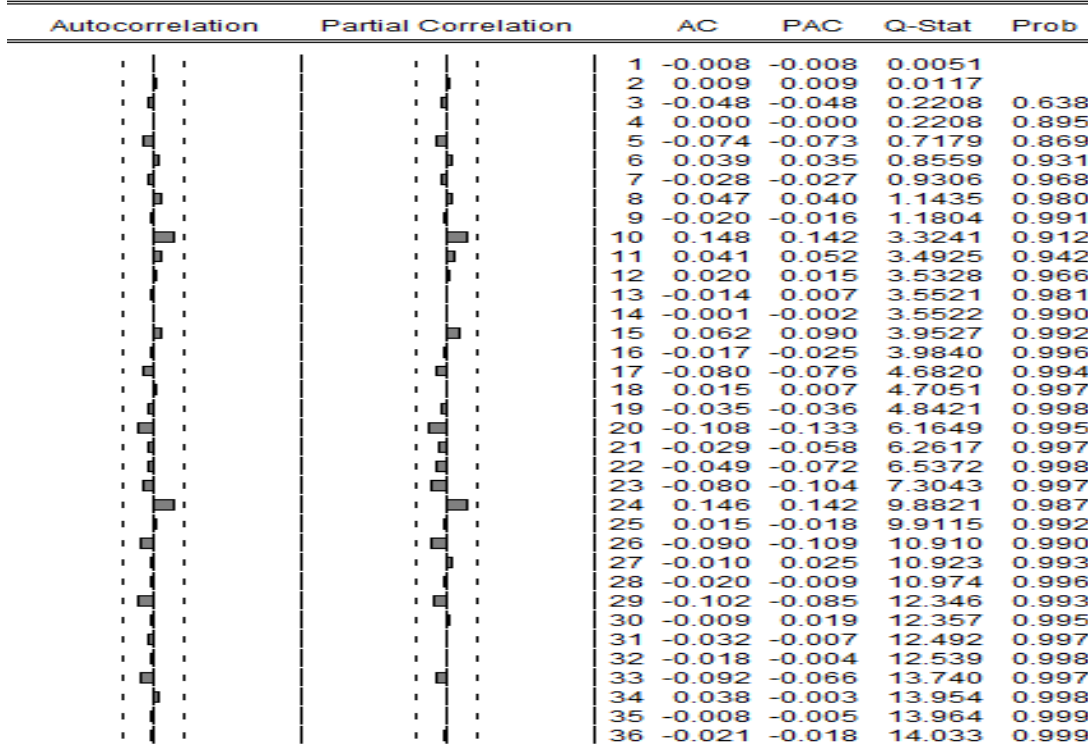


Fig 4. Ljung-Box Q test of the residual

Conclusion

In this study we empirically evaluated the ARIMA model that will be appropriate for forecasting the monthly birth rate in Bayelsa State, Nigeria. The time plot of the series shown in Figure 1 follows an irregular sig-sag pattern showing both upward and downward movement. The Augmented Dickey Fuller test revealed that the monthly time series of birth rates contains unit root. The data was seen to be stationary in the first difference. An appropriate forecasting model was obtained using the Box-Jenkins method. Based on the behavior of ACF and PACF plots, the ARIMA (1,1,1) model was identified as the most adequate model. The model adequacy was confirmed through Ljung-Box Q test. The residual of the model was checked using Ljung-Box and it shows no sign of autocorrelation in the residual. We recommend that further studies should be carried out on forecasting Bayelsa State’s monthly birth rate using the model.

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